

Errata: Elements of Phase Transitions and Critical Phenomena

6 April 2011

Important corrections

Overall: In the first print, the symbol “ \neq ” is misprinted as “ $/ =$ ”. Corrected in the second print.

p. 49 In eqs. (2.121), (2.122) and the last line, b is to be replaced by $2b$.

p. 50: In eqs. (2.123), (2.125), and (2.128), b is to be replaced by $2b$.

p. 133: In eq. (6.22), the second term on the first line. The arguments of $\phi_j(z, \bar{z})$ should be replaced as $\phi_j(f, \bar{f})$.

p. 156: The footnote is to be deleted.

p. 162: Replace eq. (7.31) by the following expression and statements:

$$\begin{aligned}\langle (\phi(r) - \phi(0))^2 \rangle &\approx \frac{T}{J} \int \frac{2 - e^{i\mathbf{q}\cdot\mathbf{r}} - e^{-i\mathbf{q}\cdot\mathbf{r}}}{q^2} \frac{d\mathbf{q}}{(2\pi)^2} \\ &= \frac{T}{(2\pi)^2 J} \int_0^{a^{-1}} \frac{dq}{q} \int_0^{2\pi} (2 - e^{iqr \cos \theta} - e^{-iqr \cos \theta}) d\theta \\ &= \frac{T}{(2\pi)^2 J} \int_0^{a^{-1}} \frac{dq}{q} (4\pi - 4\pi J_0(qr)) \\ &= \frac{T}{\pi J} \int_0^{a^{-1}} \frac{dq}{q} (1 - J_0(qr)) = \frac{T}{\pi J} \int_0^{r/a} \frac{dy}{y} (1 - J_0(y)) \\ &= \frac{T}{\pi J} \left(\int_0^1 \frac{1 - J_0(y)}{y} dy + \int_1^{r/a} \frac{dy}{y} - \int_1^{r/a} \frac{J_0(y)}{y} dy \right)\end{aligned}$$

where $J_0(qr)$ is the Bessel function. The first term of the last line is independent of r , the second term is $\log(r/a)$, and the third term approaches a constant in the limit $r \rightarrow \infty$. Therefore, for $r \rightarrow \infty$, the first and third terms can be neglected in comparison with the second term, and the above equation reduces to

$$\langle (\phi(r) - \phi(0))^2 \rangle \approx \frac{T}{\pi J} \log\left(\frac{r}{a}\right) \quad (7.31)$$

p. 183: In the footnote, the whole expression $J \cos \Delta\theta - J \cos 0$ should be multiplied by -1 .

Minor typos

p. 30: Just below eq. (2.34), $i = 1, 2, \dots, N$ and $j(\neq i) = 1, 2, \dots, N$ should read $i = 1, 2, \dots, N$ and $j(\neq i) = 1, 2, \dots, N$. (Commas are inserted.)

p. 157: In eq. (7.7), $e^{-i\mathbf{q}_1 \cdot \mathbf{r}}$ and $e^{-i\mathbf{q}_2 \cdot \mathbf{r}}$ should be $e^{i\mathbf{q}_1 \cdot \mathbf{r}}$ and $e^{i\mathbf{q}_2 \cdot \mathbf{r}}$.

- p. 157: In eq. (7.9), $e^{-i\mathbf{q}\cdot\mathbf{r}}$ should be $e^{i\mathbf{q}\cdot\mathbf{r}}$.
- p. 157: Just above eq. (7.10), $e^{-i\mathbf{q}\cdot\mathbf{r}} \approx 1$ should be $e^{i\mathbf{q}\cdot\mathbf{r}} \approx 1$.
- p. 185: In eq. (8.20), all $d\mathbf{q}$ are to be replaced by $\frac{d\mathbf{q}}{(2\pi)^d}$.
- p. 210: In eq. (9.36), $\lambda+$ " should read λ_+ .
- p. 212: In eq. (9.45), $(S_{N_1})^2 + (S_{N_2})^2 + \cdots + (S_{N_n})^2 - 1$ should read $(S_{N_1})^2 + (S_{N_2})^2 + \cdots + (S_{N_n})^2 - 1$.
- p. 226: In eq. (9.104), $\pm \frac{2\pi}{L}$, , should read $\pm \frac{2\pi}{L}$,.
- p. 274: Just below eq. (A.36), e^{ixk} should be e^{ikx} .